

The coordinates of $P_0 = (0, 0)$ and of $P_4 = (1020, 0)$ are known but the coordinates of the points P_1 , P_2 and P_3 must be determined.

To determine the coordinates of a point P , measure the distances from $P = (x_P, y_P)$ to two points with known coordinates, $A = (x_A, y_A)$ and $B = (x_B, y_B)$.

If we call the distances between P and A and P and B L_A and L_B respectively, we get the following equation system where the equations describe two circles with centers in A and B and with radii given by L_A and L_B .

$$\sqrt{(x_P - x_A)^2 + (y_P - y_A)^2} = L_A \quad (1)$$

$$\sqrt{(x_P - x_B)^2 + (y_P - y_B)^2} = L_B. \quad (2)$$

This system of equations has two solutions (intersection points) where there are two points, P and Q , which are both at the same distance from points A and B . In this case it is point P , the right intersection we are interested in. See Figure 2.

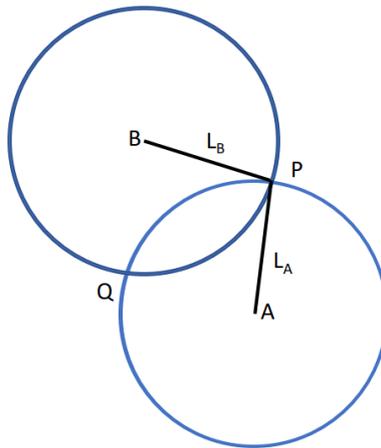


Figure 2: Determination of coordinates for the point P with binding. The coordinates of the points A and B and the lengths L_A and L_B are known.

1a) Start by determining the coordinates (with the appropriate tolerance) for points P_1 , P_2 and P_3 using binding. For each point, a non-linear system of equations must correspond (1) - (2) is solved by Newton's method. Initial values are determined by drawing the circles.

The table below shows points A and B with known coordinates and measured distances between A and P and B and P for points P_1 , P_2 and P_3 .

The coordinates are given in meters from the point (0, 0).

The program should not use code repetition. Use a **for-loop** for the three points. **Report the coordinates and that Newton's method converges squarely.**

P	$A = (x_A, y_A)$	$B = (x_B, y_B)$	L_A [m]	L_B [m]
P_1	(175, 950)	(160, 1008)	60	45
P_2	(410, 2400)	(381, 2500)	75	88
P_3	(675, 1730)	(656, 1760)	42	57

1b) Determine the fourth degree polynomial, $p(x)$, which passes through the five points P_0 , P_1 , P_2 , P_3 and P_4 . **Draw the path (graph of the polynomial) for $x \in (0, 1020)$. Also draw the five the interpolation points and mark them with 'o'. Report the coefficients in the polynomial and the figure with the plotted path and the interpolation points.**

1c) Calculate the length of the new road from the point (0, 0) to the point (1020, 0). Use the trapezoidal rule with the appropriate step length. **Report the length of the road and that your implementation of the trapezoidal rule has an accuracy order 2. Tip: how do you calculate the arc length of a curve?**

1d) Assume the lengths L_A and L_B have an uncertainty of ± 5 m. **Calculate the uncertainty length on the road with experimental disturbance calculation. Report the uncertainty in the length calculation.**

Tip: For the experimental disturbance count, the code that solves a) -c) is packaged in a **"black box "**(a Matlab function) that takes L_A and L_B for the three points that input and gives the length of the path as output.