



# IEBE Assignment

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## Question 1

**#First, the author imports three R packages.**

```
library(sjPlot)
```

```
library(see)
```

```
library(performance)
```

**#Then, the author creates a dataframe based on the NervloveData**

```
Data = as.data.frame(NervloveData)
```

**#The author create the model of q1 by the following code**

```
logTC=log(Data$totcost)
```

```
logQ=log(Data$output)
```

```
logPL=log(Data$plabor)
```

```
logPF=log(Data$pfuel)
```

```
logPK=log(Data$pkap)
```

```
q1model = lm(logTC ~ logQ + logPL + logPF + logPK)
```

**#Then, the author use "tab\_model" to make a table of the model**

```
tab_model(q1model)
```

costs in 1970, MM USD			
<i>Predictors</i>	<i>Estimates</i>	<i>CI</i>	<i>p</i>
(Intercept)	-3.53	-7.03 – -0.02	<b>0.049</b>
log(Data\$output)	0.72	0.69 – 0.75	<b>&lt;0.001</b>
log(Data\$plabor)	0.44	-0.14 – 1.01	0.136
log(Data\$pfuel)	0.43	0.23 – 0.62	<b>&lt;0.001</b>
log(Data\$pkap)	-0.22	-0.89 – 0.45	0.518
Observations	145		
R <sup>2</sup> / R <sup>2</sup> adjusted	0.926 / 0.924		

**#Interpret the estimated coefficients in the log-log equation.**

#Xi increase by 1 %, Yi change by  $\beta_1\%$ , coefficients are elasticities

#Output increase by 1 %, Cost change by 0.72%

#Labour increase by 1 %, Cost change by 0.44%

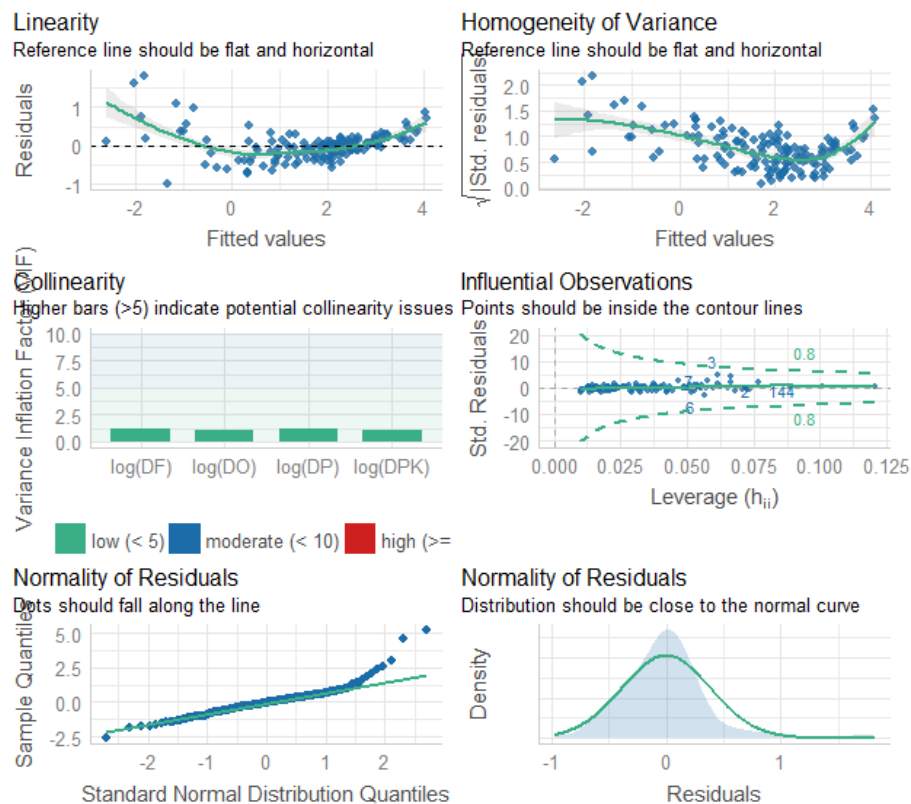
#Fuel increase by 1 %, Cost change by 0.43%

#Capital increase by 1 %, Cost change by -0.22%

#Is the OLS coefficient unbiased?

#Use "check\_model" to check its obey to the assumptions

check\_model(q1model)



#There are three assumptions needed to be fulfilled for unbiased:

#No multicollinearity: fulfilled as no bars higher than 5

#Strict exogeneity: Not fulfilled, the variance of residuals change with the regressors

#Linearity: Not fulfilled as the reference line is not flat nor horizontal.

#Hence, as two out of three assumptions are not fulfilled, this model is biased.

**#What they do represent in practice?**

#They are elasticities that shows the percentage reaction of the Y to the regressors

**Test the coefficients and comment on the obtained results**

```
tab_model(q1model)
```

#In the output diagram, two predictors statistical meaningfully positive affect the cost

#that logged output ( $p < 0.001$ ) and logged fuel price ( $p < 0.001$ )

#Labor and Capital has a high p-value, hence no evidence to reject the null hypothesis

#that they have no meaningful effect on the dependent variable.

**Question 2****#Check the correlations**

```
cor(Data[,2:5])
```

**#Inspecting the correlation between variables**

#there are no linear relationships among the variables

#Hence, the model is unlikely to be affected by multicollinearity

```
vif(q1model)
```

#The author further verifies this conclusion by this function. As no value is higher than 5, the author concludes that no multiple colinearities

**#What does multicollinearity do to your regression?**

#Multicollinearity disobeys the assumption that "No linear relationships among the variables". Hence the regressor matrix does not have full ranks. As the calculation of the OLS estimator needs to use  $X'X$ , the multicollinearity prevent us from calculating the OLS estimator. However, Multicollinearity does not affect the overall fit.

**3. Test again the coefficients by using heteroskedasticity-robust standard errors****4. Test also the homogeneity restriction**

```
linearHypothesis(q1model,"log(DP)+log(DF)+log(DPK)=1")
```

5. In particular, write the hypothesis in the form  $R\beta = r$  and calculate the F-statistics

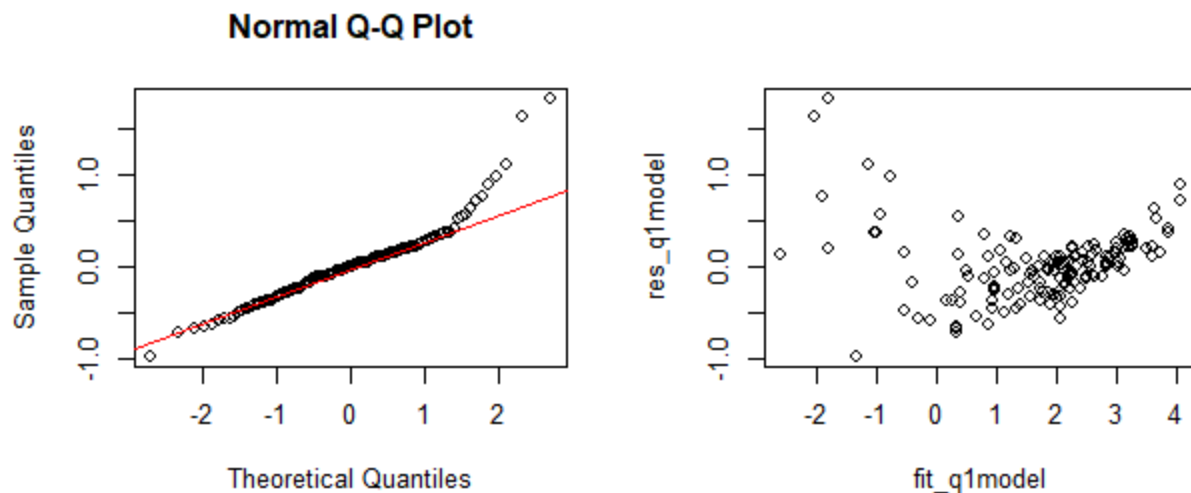
### Question 3

# No linear relationships among the variables:

```
par( mfrow = c(2 , 2) )
```

```
fit_q1model <- fitted(q1model)
```

```
res_q1model <- residuals(q1model)
```



What can we learn from these two graphs? Are the OLS assumptions satisfied? In particular, verify the following assumptions:

#### Strict exogeneity?

Spherical error variance is disobeyed due to the disobey to the homoskedasticity

Fourth moments conditions (no outliers) - (How to check outliers)

### Question 4

```
library(ggplot2)
```

```
ggplot(data= NULL, aes(x = logQ, y = res_q1model)) +
```

```
geom_point(color = "darkred")
```

## Question 5

```
q5model = lm(logTC~logQ+l(logQ*logQ)+logPL+logPF+logPK,data=data)
```

```
summary(q5model)
```

```
fit_q5model = fitted(q5model)
```

```
res_q5model = residuals(q5model)
```

```
qqnorm(scale(res_q5model, center = TRUE, scale = TRUE)) # are the residuals  
approximatively Gaussian?
```

```
qqline(scale(res_q5model, center = TRUE, scale = TRUE), col="red")
```

```
plot(fit_q5model, res_q5model, pch=c(16), lwd=2, # Residuals Vs Fitted  
     col=c("black"), xlab="Fitted values", ylab="Residuals",  
     main="Residuals Vs Fitted")
```

```
abline(0,1, col="red")
```

## Question 6

**#first, the author extract the data of five quantiles**

```
q1data = subset(Data, Data$output<quantile(Data$output,0.2))
```

```
q2data = subset(Data,  
Data$output>quantile(Data$output,0.2)&Data$output<quantile(Data$output,0.4))
```

```
q3data = subset(Data,  
Data$output>quantile(Data$output,0.4)&Data$output<quantile(Data$output,0.6))
```

```
q4data = subset(Data,  
Data$output>quantile(Data$output,0.6)&Data$output<quantile(Data$output,0.8))
```

```
q5data = subset(Data,  
Data$output>quantile(Data$output,0.8)&Data$output<quantile(Data$output,1.0))
```

```
install.packages("stargazer")
```

```
library(stargazer)
```

```
stargazer(q1data, type = "text", title="Descriptive statistics", digits=1)
```

```
stargazer(q2data, type = "text", title="Descriptive statistics", digits=1)
```

```
stargazer(q3data, type = "text", title="Descriptive statistics", digits=1)
```

```
stargazer(q4data, type = "text", title="Descriptive statistics", digits=1)
```

```
stargazer(q5data, type = "text", title="Descriptive statistics", digits=1)
```

## Question 7

**#Based on the five quantiles, the author constructed five models**

```
q7fit1 = lm(log(totcost)~log(output) + I(log(output)*log(output)) + log(plabor) + log(pfuel) +  
log(pkap), data=q1data)
```

```
summary(q7fit1)
```

```
q7fit2 = lm(log(totcost)~log(output) + I(log(output)*log(output)) + log(plabor) + log(pfuel) +  
log(pkap), data=q2data)
```

```
summary(q7fit2)
```

```
q7fit3 = lm(log(totcost)~log(output) + I(log(output)*log(output)) + log(plabor) + log(pfuel) +  
log(pkap), data=q3data)
```

```
summary(q7fit3)
```

```
q7fit4 = lm(log(totcost)~log(output) + I(log(output)*log(output)) + log(plabor) + log(pfuel) +  
log(pkap), data=q4data)
```

```
summary(q7fit4)
```

```
q7fit5 = lm(log(totcost)~log(output) + I(log(output)*log(output)) + log(plabor) + log(pfuel) +  
log(pkap), data=q5data)
```

```
summary(q7fit5)
```

```
plot(compare_performance(q7fit1, q7fit2, q7fit3, q7fit4,q7fit5))
```

